

The Science of Galaxy Formation

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Abstract. Our knowledge of the Universe remains discovery-led: in the absence of adequate physics-based theory, interpretation of new results requires a scientific methodology. Commonly, scientific progress in astrophysics is motivated by the empirical success of the “Copernican Principle”, that the simplest and most objective analysis of observation leads to progress. A complementary approach tests the prediction of models against observation. In practise, astrophysics has few real theories, and has little control over what we can observe. Compromise is unavoidable. Advances in understanding complex non-linear situations, such as galaxy formation, require that models attempt to isolate key physical properties, rather than trying to reproduce complexity. A specific example is discussed, where substantial progress in fundamental physics could be made with an ambitious approach to modelling: simulating the spectrum of perturbations on small scales.

Keywords. Galaxy: formation, Galaxy: disk, sociology of astronomy, elementary particles

1. The Scientific Method

Astrophysics challenges the limits of our scientific methodologies. We have no control over what Nature allows us to ‘observe’, and much of what we can observe involves complex non-linear physics. At the same time, astrophysics challenges the limits of our concepts of “reality”, so that our adopted methodology is important. Significant astrophysical queries include the form(s) of the dominant types of matter in the Universe, the nature of zero-point energy, and, what may be related, the interpretation of the observed acceleration of the expansion of the Universe, among other Big Questions. The appropriate scientific methodology with which to address such questions is itself problematic: how does one apply what many consider the “traditional scientific method”, involving objective analysis of independent repeated experiments as a test of theory, when the Universe does not allow us to experiment, in the traditional laboratory physics sense; when we have no useful predictive theory for much of astrophysics; and when the nature of the Universe may restrict our observation to only a very small part of an unobservable larger whole? More specifically, is the observational test of prediction how science actually operates? Is that how astrophysics operates?

The scientific method as popularly conceived is essentially the application of reason to experience, independent of authority. This concept has a long and complex evolutionary history, with many notable figures in its history, from classical Greece, through Ibn Tufayl (see eg Cerdá-Olmedo (2008)), William of Occam’s “Entia non sunt multiplicanda praeter necessitatem”, Francis Bacon’s discourse in his “Novum Organum”, Copernicus, Galileo and many more great scientists and philosophers. In his paper to the Royal Society in November 1801, “On the theory of light and colours”, Thomas Young updates Newton’s “Hypotheses non fingo” in his introduction by “Although the invention of plausible hypotheses, independent of any connection with experimental observations, can be of very little use in promotion of natural knowledge... ”, before introducing what we now know as one of the great successes and great challenges of the scientific method,

that light behaves as both a wave and a particle. Niels Bohr, when becoming a Knight of the Elephant in 1947, adopted the motto “*Contraria sunt Complementa*” (opposites are complementary), recognising the more general importance of wave-particle duality in quantum mechanical descriptions of Nature.

This raises two of the more unexpected consequences of application of the scientific method - is there such a concept as a single “answer”, and do the resulting theories describe how the world “really is”? How can they, if apparently inconsistent descriptions are both valid? Is there such a thing as “truth” in science or Nature? Again to quote Bohr “It is wrong to think that the task of physics is to find out how Nature is. Physics concerns what we say about Nature”. Or, among many hundreds of similar discussions of the meaning of probability and the role of the observer in quantum mechanics, von Neumann notes the prime requirement of a model is that “it is expected to work”. It may well be that abandoning the classical notion of “realism” is the latest step we must take in our Copernican path to remove observer-specific influence and authority from our application of reason to some generalised concept of experience (*cf* the discussion in Leggatt (2008)).

Astrophysicists are traditionally proud of their special role in what is often called the “Copernican Principle”, the scientific methodology which applies scepticism to any model of a phenomenon in which there is a special role for the observer and/or interpreter. This methodology in astrophysics, and the name, is derived from empirical “success”. Removing the special place for Mankind as the focus of all creation led to a sequence of models, ranging from Newtonian gravity, through general relativity, to modern precision cosmology. Along the way the Earth lost its central place in the Universe, followed by the Sun, then the Milky Way Galaxy. The concept of absolute time vanished, baryonic matter was dethroned by dark matter, mass-energy became secondary compared to dark energy. This last step is a significant extension of the Copernican Principle. If current speculations on long-term futures in a Universe dominated by dark energy, Multiverses, and so on, are relevant to “reality”, the Universe may well be a concept in which what we see, and what we are, is a temporary fluctuation on what, for most of space-time, may be very, very different. Cosmic variance becomes not a consideration but the dominant factor limiting understanding. We, as observers, may be seeing - or may only be able to see - an extremely unusual, temporary, microstate, and have no direct knowledge of a much, much, larger macroscopic “reality”.

For practising scientists, it is a matter of scientific habit that a “theory” which predicts a previously-unobserved phenomenon is considered supported by experiment. This overstates the case. While a positive outcome is certainly not neutral, in that the opposite outcome would lead to quite different reactions, no set of experiments can ever establish the “truth” of any theory. Even if theory **T** predicts outcome **O**, and **O** is observed, **T** is *not* proven. If **O** were outlandish, but observed, it is commonly assumed that **T** is more likely to be correct. While a successful test justifies continued use, and future testing, of that theory, **T** remains unproven. Supporting the correctness of **T** given the observation of **O** is the fallacy of “affirmation of the consequent” (*cf.* Leggatt (2008) for further discussion).

There is no fundamental theory supporting the validity of application of the “Copernican Principle”. It is an assumption, whose future validity, and whose valid range of applications, is unknowable. It may well be limited. There is certainly no objective justification for its application in fields beyond those few where it has proven utility. As an illustration, public reaction to evolutionary biology, and the scientific realisation that modern, Cro-Magnon man has been painting caves and doing science for some 10^{-5} of the age of the Earth, remains of considerable complexity, and illustrates well the dif-

ficulty many people have in acting as dispassionate “Copernican” observers. There are indeed fields of intellectual enquiry where objective analysis, independent of the concept of authority, is inappropriate. A particularly interesting example is the debate in legal and political circles of the role of the US Supreme Court in interpreting the US Constitution. Many distinguished legal theorists insist that a positivist interpretation of what is written, free from the preferences of specific judges, is most appropriate. Others disagree. This debate intriguingly combines the concepts of an authoritative document, and an objective observer and interpreter. The creativity, sophistication, and continuation, of this debate illustrates the complexity of the issues. In micro-physics the meaning and role of the “observer” in Young’s “experimental observations” and the concept of uniqueness, and/or completeness, of possible observations, have become more complex with developments in quantum mechanics. The continuing public interest in debating the validity of string theory as a science (eg Cartwright & Frigg (2007)) is yet another illustration of both the importance of the questions, and the incompleteness, or at least complexity, of current interpretations of the terms “science”, “scientific method”, “theory” and “truth”.

2. The Scientific Method in Galaxy Formation

With that context, it is perhaps unsurprising that astrophysics is implemented in a practical approximation to the philosophic ideal. Many great names in the development of twentieth century science declared, in essence, “don’t worry too much about the philosophy, just find, and use, equations which calculate observables”. Preferably previously un-predicted observables. In that context, what do we do, and what should we do, in astrophysics.

In practise, we adopt a paradigm, or set thereof, develop it/them in so far as is possible, testing against, and - hopefully - predicting, new observables. In that context significant advances have been made. In astro-particle physics, the interplay between solar structure models and neutrino astronomy is an exceptional example, as is the limitation of the numbers and masses of neutrinos from large scale structure studies. Steady State cosmology is another exceptional example – predictions were made, tested against observations, and the model found to be inappropriate as a description of the Universe. Science at its best. Such examples are however rare. Much of astrophysics either has no *ab initio* theory, or involves complex non-linear physics, so that robust and unique prediction is impossible. Given our experimental inability to isolate and test models of individual physical processes, since we are unable to experiment, we cannot “test” the outcome of a theory in astrophysics.

Much of what we do in astrophysics is similar to weather forecasting: weather forecasts use observations as boundary conditions, implement the most sophisticated available physics essentially as an interpolation (in space, in time,...), exploit heroic achievements in computing, and extrapolate the observables to other places and times. Sometimes this is accurate, sometimes not, in which case the differences between prediction and observation are analysed to allow the forecasting system to be improved. Eventually, given enough data, and enough complexity in the model, weather forecasts will become, asymptotically, as accurate as the predictability of the system allows. They will reach a physical accuracy limit. But no weather forecast can ever be “right” or “wrong”, in the sense that a scientific theory can be. A forecast may be accurate, or less accurate. It is unlikely even that any forecasting system could ever be unique, since there may well be many physical processes whose effects are comparable in amplitude to measurement error. A system with considerable complexity, and inevitable approximation, will invariably have many statistically-indistinguishable solution maxima.

Coming specifically to models of galaxy formation, we have a similar situation. There is an interesting distinction between (some) Galaxy (ie, Milky Way) models and (some) galaxy (ie generic) models. Substantial progress is being made in development of specific models of the Milky Way Galaxy, particularly in preparation for Gaia. Gaia will produce information from which we expect to determine the current state of the Milky Way Galaxy in some detail, and hence to deduce something of how the Milky Way in particular, and, *modulo* cosmic variance, disk galaxies in general, formed and evolved. A systematic approach to modelling, analysing and interpreting the anticipated Gaia data is underway. The adopted strategy is to proceed through a sequence of models of increasing complexity, guided at each stage by analysis of mis-matches between the current model and available simulations, real data and on-going surveys, such as RAVE (see eg Binney (2002), as one example of the many underway). This process is intended to develop what is essentially a tool-kit for investigation of the Gaia dataset, and hence the Milky Way Galaxy. This modelling approach is, in a real sense, equivalent to a laboratory experiment, rather than being development of a theory.

Formation models for galaxies in general are very different in approach and ambition. They adopt analyses of the properties of the early universe, derived from observations of the cosmic microwave background, and supplementary data, as boundary conditions. These boundary conditions are unconstrained by observations on small scales, and so are extrapolated [usually as a simple power-law spectrum of fluctuations] down to as-yet unobserved physical length scales. This extrapolated set of boundary conditions is then evolved forward in time, requiring considerable sophistication and heroic achievements in computing. Approximations to the behaviour of baryons, and hence the properties of most observables, are then added. Comparison with observations of real galaxies, when made, has so far invariably identified gross discrepancies, indicating perhaps that more complex baryon physics is needed. Or different physics: perhaps the extrapolation of the observational boundary conditions is inappropriate? Unfortunately, analysis and interpretation of the predictions of these inevitably highly idealised models is complex.

In order to calculate “observables” *ad hoc* prescriptions for the key baryonic physics must be added by hand. Star formation, chemical elements, black holes and so on are added using some observationally motivated recipe. After unsuccessful comparison to observation, the complexity is increased, including both plausibly anticipated and some quite *ad hoc* effects – bias, scale-dependant bias, feedback, AGN feedback, ... etc, are included. The complexities of “post-formation” dynamical evolution (or even survival) must all be approximated. And so on. Considerable current effort is involved in adjusting the non-linear aspects of the baryonic physics to try to regain consistency with observation. Consistency with observation is not a natural feature of extant models of galaxy formation.

The development of the currently available sophisticated galaxy models is a powerful and extremely impressive achievement. Is it developing a theory? There is no *ab initio* theory, no first-principles calculation, of many of the physical processes. It is feasible that a model can be identified, with eventual sufficient complexity, which is able to reproduce all extant observables. This will not be a theory. It will never be “right” or “wrong”. Until key parameter space is investigated, no model will even be unique within its limited starting points and methodology. That is, there is a fundamental distinction between development of a model/tool-kit which is appropriate to investigate Gaia-like data sets, and modelling galaxy formation from linear perturbations early in the Universe. The latter models can never be compared to data, except after ‘processing’ through complex non-linear processes, which are themselves neither understood nor quantified.

So is there any point in devoting effort to building complex models of galaxy forma-

tion, when they are inherently untestable and not unique? Yes! In fact, such modelling can, or could, already be used for important investigations of some key assumptions in general astrophysics and cosmology. Galaxy formation models, given their present (impressive) sophistication, are valuable tools to investigate hypotheses. As yet, however, the models are incapable of testing hypotheses as complex as the formation of a galaxy. Appropriate hypotheses to test are more fundamental than the highly specific challenge of adding complexity to a recipe to become not-inconsistent with extant observations. Galaxy formation models are, as yet, not very helpful tools to determine the details of the complex mix of non-linear physics which describes the evolution of baryons and dark matter on small scales in a galaxy. Galaxy formation models could however, if applied appropriately, be a very valuable tool-kit to investigate much more fundamental physics.

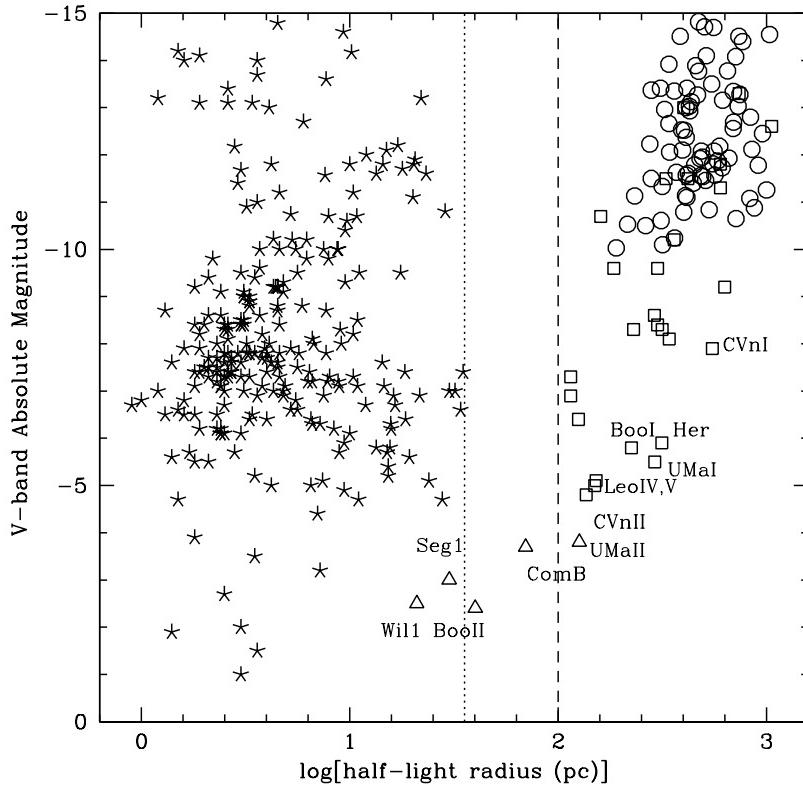


Figure 1. The relation between absolute luminosity and luminous half-light radius for small stellar systems in the local Universe. Globular clusters from several host galaxies, Ultra Compact Dwarfs, and galactic nuclei star clusters, are represented as asterisks. Local Group dSph galaxies, with the most newly discovered identified by name, are shown as open squares. Galaxies from the Local Volume survey of Sharina et al (2008) are shown as open circles. Milky Way satellites of unknown equilibrium status are shown as open triangles (see Fig 2). All equilibrium galaxies have half-light radii larger than the minimum size line at 100pc. All apparently purely stellar systems have half-light radii smaller than about 30pc. Further details are in Gilmore, Wilkinson, Wyse, et al (2007).

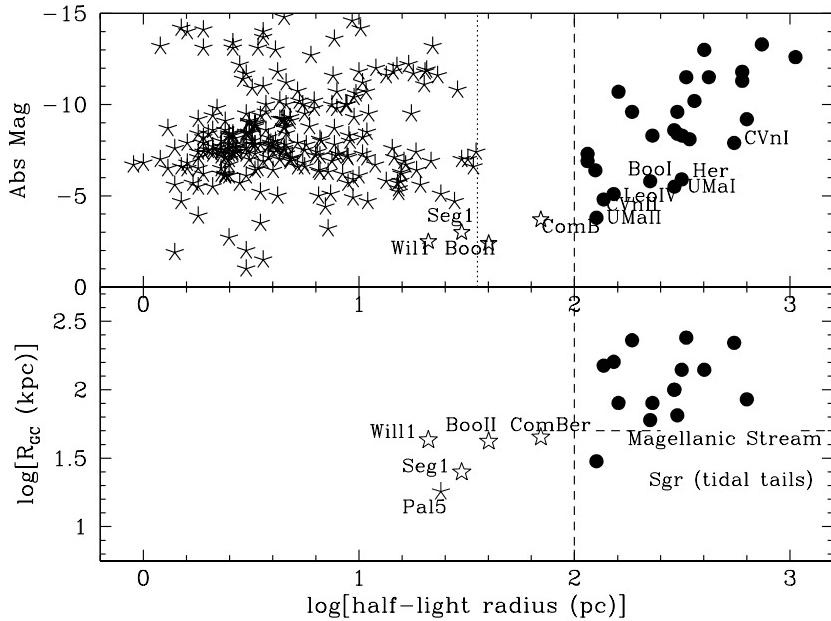


Figure 2. The observed structural properties of the smallest galaxies and stellar systems. Top: relation between absolute luminosity and luminous half-light radius. Globular clusters, Ultra Compact Dwarfs, and galactic nuclei star clusters, are represented as asterisks. dSph galaxies, with the most newly discovered identified, are shown as solid points. Objects of unknown equilibrium status are shown as open stars. All objects which show robust evidence for dark matter halos have half-light radii larger than the minimum size line at 100pc. All stellar systems have half-light radii smaller than about 30pc, and none shows evidence for dark matter. Bottom: the uncertain dynamical state of the intermediate objects is emphasised by considering size as a function of Galacto-centric distance. All uncertain objects are in a region where Galactic tides are expected to be important, and so may have time-dependent structures. Further details are in Gilmore, Wilkinson, Wyse, et al (2007).

2.1. What galaxy formation models could tell us

There are fundamental questions in physics, and in Λ CDM cosmology, which are best addressed using galaxy formation models. Applications to the fundamental properties of neutrinos are mentioned above. To give just one more important example, the standard model of particle physics is known to be incomplete. Extension to a more general theory requires guidance from observations. Recently, most of these new observations have come from astrophysics - neutrino masses, baryogenesis, matter-anti-matter asymmetry, the dominance of dark matter, the importance of dark energy, are among this list. The minimal super-symmetric extension of the particle physics standard model, which does not even encompass all the complexity required to address all the items on this list, has more than 120 free parameters. Hopefully, in the near future, CERN will advance measurement of aspects of the parameter space. Astrophysics has done so – limits on neutrino masses from large scale structure are a superb example – but can do much more, including investigating aspects of physics at a more fundamental scale than is possible with accelerators.

Perhaps the best and most immediate example is in testing the small-scale extension of the spectrum of perturbations. At present, Λ CDM models adopt the spectrum of perturbations from analysis of CMB and other observations, and extend this to zero scale. The

extension is unphysical, in being ultraviolet divergent. Suppression of the divergence is provided essentially by numerical smoothing (“finite resolution”) in cosmological simulations. It is unlikely that Nature does it that way. Rather, the small-scale power spectrum may well be where astroparticle physics comes into action on observable scales. Testing this is arguably much more interesting than is applying ingenuity to fine-tune outcomes of the models to make them not-inconsistent with already known observations.

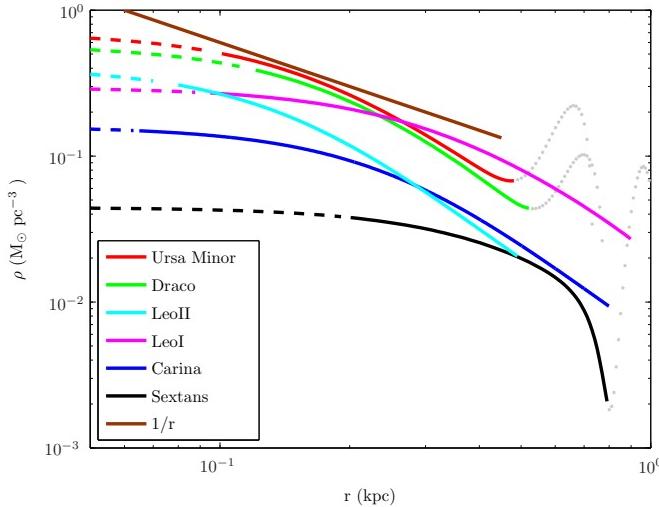


Figure 3. Derived internal mass profiles for the well-studied dSph galaxies. In each case a cored dark matter distribution is preferred by the kinematic data, with a scale radius comparable to that of the luminous scale shown in Figures 1 & 2. The similarity of this scale in all cases studied implies it is an inherent property of dark matter itself. Further details are in Gilmore, Wilkinson, Wyse, et al (2007).

A huge literature is available considering the implications of specific possibilities and elementary particle types in astrophysics. Ostriker & Steinhardt (2003) provide an accessible summary of the interplay between small-scale structure and classes of physically motivated explanations for suppression of the ultraviolet divergence. The key is that physical effects may be expected on scales of the smallest galaxies, the dSph. It is perhaps not coincidence that it is on these scales that the bottom-up galaxy formation models have proven to be most inconsistent with observations. The list of relevant issues is long, and well-known. Examples from a long list include the existence of old red massive galaxies, the Tully-Fisher relation being in place by redshift unity, the frequency of large old cold disks in galaxies, and the satellite problem. Such a long list of observations all inconsistent with apparently fundamental features of galaxy formation models suggests two approaches. In one approach, new complex physics (“feedback”) must be added, to “improve” agreement with observation. The appearances are to be saved. In another, common assumptions in the galaxy simulations could be examined further.

The recent observational status of the small-scale problem is described in Gilmore, Wilkinson, Wyse, et al (2007). An updated summary is presented in figures 1, 2, and 3 here. There are two key results: the lowest luminosity galaxies are all very dark-matter dominated, and all have an equilibrium minimum half-light optical radius of $> 100\text{pc}$. The largest star clusters have half-light radius less than 30pc. No equilibrium objects are known in the local Universe with half-light size between 30pc and 100pc (Figures 1,2). Dynamical studies of stellar kinematics in very low-luminosity galaxies all prefer a dark-matter distribution which is cored, with a mass scale length comparable to the luminosity scale length (Figure 3).

Standard assumptions adopted in simulations of galaxy formation have no presumed physical scale (ie, the UV divergence), so featureless smooth distributions are a natural feature. A specific length scale is not anticipated, but is seen. This physical scale seems to be special.

It may well be that we are discovering a physics-based solution to the medley of challenges to galaxy formation models: the divergence of the small-scale extrapolation of the perturbation spectrum is at fault. The physics of the mix of dark matter particles may be the explanation. While it will require considerable ingenuity to extend the resolution of numerical simulations to handle such small scales reliably, this is an example where simulations could explore the effect of the power spectrum, and so investigate a new regime. That is a physics experiment which really can test a physical theory: using observations of galaxies as a guide, is there an astrophysically observable physical scale at which the power spectrum converges? What is the sensitivity of predictions of galaxy formation to the assumed boundary conditions on small scales? What classes of elementary particles must then make up much of the dark matter on small scales?

2.2. A constraint on early substructure

Among the most direct measures of the size and location of early star formation is scatter in chemical element ratios (see papers here by Wyse, by Nissen, and others). Small scatter requires a large and well-mixed star-forming region, which has an independent existence for sufficiently long to self-enrich. Careful quantification of the scatter in element ratios as a function of [M/H] clearly can count the number of star-forming events in the early Galaxy directly. This is of course well known, and has been so for many years. An interesting extension of this analysis can be applied to the light elements Beryllium (and Lithium) which are made, fully for Be, partly for Li, by cosmic ray spallation, probably with CNO nuclei as cosmic ray primaries spallating onto H-nuclei (cf Pasquini, this meeting, and Gilmore, Gustafsson, Edvardsson & Nissen (1992)). This spallation involves very high-energy heavy nuclei, probably accelerated by the same supernovae in which they were created. Such high-energy particles have a very long mean free path. They cannot be retained inside a small or short-lived star forming event, such as a small, transient, dark matter halo. Thus, inevitably, any stars formed in such small halos will have little or no Be. Their Li abundances will also provide a robust determination of the relative contributions of BBN and later spallation to their Li abundances. Determination of the range of Be abundances in field halo stars, and – ideally – in either a low-mass dSph galaxy or a verifiable kinematic stream, will provide extremely interesting constraints on the range of places where early star formation occurred.

3. An historical lesson

This meeting celebrates the centenary of Bengt Strömgren. Openness to the implications of observations, and an ability to move beyond preconceptions, was one of his great attributes. My personal example involved his long-standing research interest in the formation and evolution of the Galactic disk. After decades of work, developing the Strömgren photometric system, and acquiring vast data sets, Bengt Strömgren, in retirement(!!) was near to finalising his major study of the distribution of stellar ages and abundances near the Sun. In 1983 Gilmore & Reid announced their discovery of the Galactic thick disk. The thick disk stellar population is old and relatively metal-rich [Gilmore & Wyse (1985)], with a main-sequence turn-off to the red of the F-star range which was at the time being studied in Strömgren's survey. Seeing this result, Bengt Strömgren invited me to visit, rapidly persuaded himself that his extant survey was bi-

assed by being based on a too-restrictive assumption on the past age-metallicity relation, and so extended his survey to include redder stars. He did this knowing that he might well not live to see the outcome of his lifetime research project. An impressive example of scientific objectivity, indeed. Fortunately, his colleagues worked hard, the weather was good, so Bengt Strömgren was able to present the first results of his expanded survey in his last scientific paper, Strömgren (1987).

References

- Binney, J. 2002, *EAS Publications Series, Volume 2, Proceedings of "GAIA: A European Space Project"*, held 14-18 May, 2001 Les Houches, France. Edited by O. Bienaym and C. Turon. EDP Sciences pp.245-256
- Cartwright, N. & Frigg, R. 2007, *Physics World*, 20, 14 (September)
- Cerda-Olmedo, E. 2008, *European Review*, 16, 159
- Gilmore, G., Gustafsson, B., Edvardsson, B., & Nissen, P.E. 1992, *Nature*, 357, 379
- Gilmore, G., Reid, I.N. 1983, *MNRAS*, 202, 1025
- Gilmore, G., Wyse, R.F.G. 1985, *AJ*, 90, 2015
- Gilmore, G., Wilkinson, M.I., Wyse, R.F.G., Kleyna, J.T., Koch, A., Evans, N.W., & Grebel, E.K. 2007, *ApJ*, 663, 948
- Leggatt, A.J. 2008, *RPP*, 71, 1
- Ostriker, J.P. & Steinhardt, P. 2003 *Science*, 300, 1909
- Sharina, M.E., Karachentsev, I.D., Dolphin, A.E., et al 2008 *MNRAS*, 384, 1544
- Strömgren, B. 1987 in 'The Galaxy', eds G Gilmore and R Carswell, CUP, p229.